Stress intensity factor computation of inclined cracked tension plate using XFEM

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ABSTRACT

One of the major successes in the field of Linear Elastic Fracture Mechanics (LEFM) is the groundwork of the stress intensity factor (SIF) computation. The approaches used to carry out SIF values may be analytical, semi-analytical, experimental or numerical. Each one of the above methods has its own benefits however the use of numerical solutions has become the most frequent and popular. Numerous schemes for the numerical computation of SIF have been developed, the J-integral method being the most popular one. In this article we examine the SIFs of an edge cracked two dimensional (2-D) steel plate subjected to tensile loading. Extended finite element (XFEM) computational scheme has been employed to estimate the values of SIF. The SIF values of cracks with different lengths and inclination angles (different configurations) have been examined by utilizing the domain based interaction integral approach. The effect of crack inclination and crack position on SIFs ($K_I$ and $K_{II}$) has also been studied. The results obtained in this study were compared with those from literature and theoretical values and observed that they are in close agreement.

Keywords: Inclined Cracked tension plate Mixed mode I/II Stress intensity factors (SIFs) XFEM

1. Introduction

Fracture is one of the most challenging failure modes in engineering and resulted from material instability in mechanical or structural components normal to the discontinuity (Belytschko et al., 2014). In many engineering fields, several terrible accidents are mainly originated from defects like micro-cracks and voids. Thus, research developments in the area of fracture mechanics are crucial. One of the key achievements in the field of Linear Elastic Fracture Mechanics (LEFM) is the concept of the stress intensity factor (SIF). The basic and fundamental stress intensity factor was introduced by Irwin (1957) and he investigated that SIF is a crucial parameter that uniquely describes the stress field in the neighborhood of crack tip. Additionally, SIF provides information about the direction and speed of moving crack, hence its determination is quite convenient to decide crack growth rate (Paris & Erdogan, 1963). In general, SIF is a function of crack size, crack location, geometry of specimen and magnitude and distribution of load intensity (Pais, 2011). Currently there are numerous techniques in the calculation of SIF, but the energy release approach and the field variable approach are the most frequently adopted numerical approaches to extract SIFs (Murakami & Keer, 1993; Lins et al. 2015). The energy release approach includes the J-integral (Rice, 1968) the stiffness derivative method (Parks, 1974) the Interaction
Integral Method (Moran & Shih, 1987) the virtual crack extension method (Hellen, 1975) the Contour Integral Method (Stern et al., 1976; Szabo & Babuška, 1988) and the virtual crack closure technique as developed by (Rybicki & Kanninen, 1977). The field variable approaches on the other hand can be segmented into stress based techniques and displacement based techniques. The displacement based technique encompasses the quarter-point displacement method (Barsoum, 1974; Henshell and Shaw, 1975) and the displacement correction method (Shih et al., 1976). Based on the principles of LEFM, Finite Element Method (FEM) (Han et al., 2015; Fayed, 2017; Leung et al., 2014; Bhadauria et al., 2010; El Fakkoussi et al., 2019) and Boundary Element Method (BEM) (Gonzalez et al., 2015; Ortiz & Cisilino, 2006; Portela et al., 1992) have been widely employed for years to determine SIFs.

It is well known that flaws like scratches, micro-cracks or other forms of discontinuities are inevitable during the fabrication of mechanical components. These discontinuities considerably affect the performance of a component by creating theoretically infinite stresses near the crack tip. The presence of discontinuities also creates interruption of operation, failure or even terrible accidents. Therefore, it is vital to give attention to the design and analysis of mechanical components with flaws. One of the most versatile and flexible numerical tools that solve a variety of engineering problems in the history of computational mechanics is the finite element method (FEM). While FEM is an effective and well established method of solving engineering problems, it has got its own constraints in the modeling and analysis of fracture problems (Belytschko & Black, 1999). One major constraint of the method is its dependency on mesh density. To capture the field variables near the crack tip FEM requires a fine and conformal mesh. Furthermore in the case of moving cracks FEM demands remeshing whenever the crack moves. To bypass the above restrictions faced by standard FEM, researchers proposed both meshless and mesh based (Belytschko et al., 1994; Belytschko et al., 1994; Lu et al., 1994; Liu et al., 1995; Rabczuk & Belytschko, 2004; Ching & Yen, 2005; Gu et al., 2011; Lee et al., 2016) numerical schemes. (Moes et al., 1999) pushed forward the standard FEM by adding an enrichment function with additional degrees of freedom at the crack surfaces and crack tip. For the last two decades researchers have significantly studied XFEM as a solution tool in area of engineering and science due to its versatility in simplifying problems with discontinuities (Belytschko & Black, 1999; Moes et al., 1999; Menk & Bordas, 2011; Singh et al., 2012; Bouhala et al., 2013; Ameri et al., 2021; Mirmohammad et al., 2018, Aliha et al., 2016;2020,2021). In XFEM the standard FEM equations are supplemented with additional functions called enrichment functions. SIF computation of a slanted central crack of aluminum plate using ABAQUS XFEM package has been demonstrated in (Hedayati & Vahedi, 2014). In this article the authors estimated the life of the structure using ABAQUS XFEM tool. Similarly (Laftah, 2016) used the general finite element software ABAQUS to study the influence of crack length on the determination of SIF of corrugated plate. Therefore, the aim of this article is to develop XFEM formulation to compute the stress intensity factor of 2-D steel plates with edge cracks at different locations and angular positions. In this study, the effect of crack orientation angles and positions on the SIFs will also be considered. Mode I/II SIFs at different crack locations along the height of the plate were studied. In this article the domain based interaction integral scheme has been implemented on MATLAB to compute the SIFs. To the best of the authors’ knowledge no one studied the SIF determination of slant cracked steel plate using XFEM by taking into account the indicated parameters.

2. Properties and Model Geometry of Plate

For demonstration purpose a plate having an edge crack with different inclination angles $\beta$ subjected to tensile loading has been considered as shown in Fig. 1. Inclined crack geometry and its boundary conditions are also illustrated in Fig. 1. The bottom edge of the plate is constrained in the y direction and the top edge is subjected to uniform tensile stress of $\sigma_t = 10$ MPa. The following dimensions and material properties are considered. The dimensions and material properties of the plate for this study are adopted from (Fayed, 2017) where the height of the plate (2D) is 20 cm, and its width (L) is 10 cm. Furthermore, the elastic modulus (E) and Poisson’s ratio (v) are 206 GPa and 0.3, respectively. In this study, crack length to width ratios ($a/L$) of 0.1, 0.2, 0.3, 0.4, and 0.5 has been considered with that of variations in the
crack angle $\beta$ between $0^\circ$ and $75^\circ$. The crack angle $\beta$ measured counterclockwise with reference to the horizontal axis. The other parameter considered in this study was the relative crack positions along the height ($d/D$) ranging from 0 to 0.7 with 0.1 increments were analyzed.

![Fig. 1. Dimensions and boundary conditions of an edge cracked tension plate.](image)

3. Numerical implementation and Governing Equation

Consider a body with domain $\Omega$ which is bounded by $\Gamma$. The boundary $\Gamma$ comprises displacement ($\Gamma_u$), traction free ($\Gamma_e$) and traction ($\Gamma_t$) boundary conditions as depicted in Fig. 2. According to (Pommier et al., 2011) the equilibrium equations are expressed as:

$$\nabla \cdot \sigma + b = 0 \quad \text{in } \Omega \quad (1)$$
$$\sigma \cdot n = \bar{F} \quad \text{on } \Gamma_t \quad (2)$$
$$\sigma \cdot n = 0 \quad \text{on } \Gamma_e \quad (3)$$

where, $\sigma$, $b$, $\nabla$ and $n$ represent stress tensor, body force per unit volume divergence operator and outward normal respectively. The following kinematic equations may be applied for small displacements:

$$\varepsilon = \varepsilon(u) = \nabla_s u \quad (4)$$

Its boundary condition is

$$u = \bar{u} \quad \text{on } \Gamma_u \quad (5)$$

where, $\varepsilon$, $u$ and $\nabla_s$ denote strain, displacement vector and the symmetric portion of gradient operator respectively.

![Fig. 2. Domain with crack and different boundary conditions.](image)
For linearly elastic materials the constitutive relation is given as:

$$\sigma = D \varepsilon$$

where $\varepsilon$ is the strain and $D$ is Hook's tensor and it is given as follows:

$$D = \frac{E}{(1+\nu)(1-2\nu)} \begin{bmatrix} 1-\nu & \nu & 0 \\ \nu & 1-\nu & 0 \\ 0 & 0 & 1-2\nu \end{bmatrix} \quad \text{plane strain}$$  \hspace{1cm} (7)

$$D = \frac{E}{1-\nu^2} \begin{bmatrix} 1 & \nu & 0 \\ \nu & 1 & 0 \\ 0 & 0 & 1-\nu \end{bmatrix} \quad \text{plane stress}$$  \hspace{1cm} (8)

In Eq. (7) and Eq. (8) $\nu$ and $E$ represent Poisson’s ratio and Young’s modulus respectively. The weak form of governing equilibrium equation can be written as:

$$\int_{\Omega} \sigma (u) : \varepsilon (v) d\Omega = \int_{\Omega} b_v d\Omega + \int_{\Gamma} t_v d\Gamma$$  \hspace{1cm} (9)

Fig. 3 shows the graphical representation of split elements that are enriched with Heaviside function (red circles) and tip elements enriched with complex functions (blue squares).

**Fig. 3.** Nodes enriched with Heaviside and crack tip functions.

### 3.1 Edge Crack Modeling using XFEM

The XFEM mesh does not require conforming to the geometry of the crack unlike standard FEM where remeshing is mandatory and hence XFEM is quite efficient in modeling discontinuities. According to (Sukumar et al., 2001; Moes et al., 1999) displacement function for 2-D crack modeling is approximated as:

$$u^h(x) = \sum_{j=1}^{n_n} \Psi_j(x) \left[ \mathbf{u}_j + \sum_{j=1}^{n_n} \left[ H(x) - H(x_j^e) \right] a_j + \sum_{j=1}^{n_n} \beta_j \left[ \beta_j(x) - \beta_j(x_j^e) \right] b_j \right],$$  \hspace{1cm} (10)

where $\mathbf{u}_j$ is a vector related to standard FEM degrees of freedom (DOF). $n$ represents the entire nodes of the mesh, $n_n$ stands for those node sets entirely crossed by the crack, $n_i$ signifies node sets belong to
elements partly cut by the crack. \( a_j \) represents the nodal DOF supplementing Heaviside function and \( b_j \) represents the nodal DOF supplementing tip enrichment, \( \beta_\alpha(x) \).

The tip enrichment function \( \beta_\alpha(x) \) is given by:
\[
\beta(x) = \left[ \sqrt{r} \cos \frac{\theta}{2}, \sqrt{r} \sin \frac{\theta}{2}, \sqrt{r} \cos \frac{\theta}{2} \sin \frac{\theta}{2}, \sqrt{r} \sin \frac{\theta}{2} \sin \frac{\theta}{2} \right]
\]  
\( \theta \) and \( r \) are local polar coordinates. After substituting the test and trial functions into Eq. (9) and employing nodal variations arbitrariness, the following discrete equations are obtained:
\[
[K][d] = [f]
\]  
(12)

Here \( d \) is nodal unknowns’ vector, \( f \) and \( K \) are externally applied force vector and global stiffness matrix respectively. By making use of the approximation functions for a crack, which are defined in Eq. (10), the element stiffness matrix \( K_{ij}^e \) and nodal vector force \( f^e \) are obtained as follows:

\[
K_{ij}^e = \begin{bmatrix}
K_{ij}^{aa} & K_{ij}^{ab} \\
K_{ij}^{ba} & K_{ij}^{bb}
\end{bmatrix}
\]  
(13)

\[
f^e = \begin{bmatrix}
f^u_i \\
f^a_i \\
f^{b1}_i \\
f^{b2}_i \\
f^{b3}_i \\
f^{b4}_i
\end{bmatrix}
\]  
(14)

From Eq. (13) and Eq. (14), the following sub matrices are given:

\[
K_{ij}^r = \int_{\Omega^r} (B_i^r)^T D(B_j^r) d\Omega,
\]  
\( r, s = u, a, b \)  
(15)

\[
f^u_i = \int_{\Gamma^r} \Psi_j^i b^j d\Gamma + \int_{\Gamma^s} \Psi_j^i b d\Omega
\]  
(16)

\[
f^a_i = \int_{\Gamma^r} \Psi_j^i (H(x) - H(x_i)) b^j d\Gamma + \int_{\Gamma^s} \Psi_j^i (H(x) - H(x_i)) b d\Omega
\]  
(17)

\[
f^{ba}_i = \int_{\Gamma^r} \Psi_j^i (\beta_\alpha(x) - \beta_\alpha(x_i)) b^j d\Gamma + \int_{\Gamma^s} \Psi_j^i (\beta_\alpha(x) - \beta_\alpha(x_i)) b d\Omega
\]  
(18)

\( \Psi_j^i \) is standard FEM shape function, \( B_i^u, B_i^a, B_i^b \) and \( B_i^{ba} \) are shape function derivatives matrices and given below:

\[
B_i^u = \begin{bmatrix}
\Psi_{i,i} & 0 \\
0 & \Psi_{i,j}
\end{bmatrix}
\]  
(19)

\[
B_i^a = \begin{bmatrix}
\Psi_j^i (H(x) - H(x_i))_x & 0 \\
0 & (\Psi_j^i (H(x) - H(x_i))_y
\end{bmatrix}
\]  
(20)

\[
B_i^b = \begin{bmatrix}
B_i^{b1} & B_i^{b2} & B_i^{b3} & B_i^{b4}
\end{bmatrix}
\]  
(21)

\[
B_i^{ba} = \begin{bmatrix}
(\Psi_j^i (\beta_\alpha(x) - \beta_\alpha(x_i)))_x & 0 \\
0 & (\Psi_j^i (\beta_\alpha(x) - \beta_\alpha(x_i)))_y
\end{bmatrix}
\]  
(22)

\( \alpha = 1, 2, 3, 4 \)
The basic and fundamental conception of LEFM is applicable if and only if the plastic deformation at the crack tip is small. According to (Anderson, 2017) the stress state at the neighborhood of the crack front is given as

\[
\sigma_{ij} = \frac{1}{\sqrt{2\pi r}} \left[ K_I f_{ij}^I(\theta) + K_{II} f_{ij}^{II}(\theta) + K_{III} f_{ij}^{III}(\theta) \right]
\]

(23)

where \( K_I, K_{II} \) and \( K_{III} \) are SIFs for mode I (opening), II (Shear) and III (out-of-plane shear) respectively. \( f_{ij}(\theta) \) denotes dimensionless trigonometric function of \( \theta \). Stress and displacement field equations in the vicinity of the tip for the three fracture modes are summarized in Table 1 and Table 2 respectively (Anderson, 2017).

**Table 1.** Crack Tip Stress Fields for Modes I and II (Anderson, 2017)

<table>
<thead>
<tr>
<th>Mode</th>
<th>( \sigma_{xx} )</th>
<th>( \sigma_{yy} )</th>
<th>( \sigma_{xy} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mode I</td>
<td>( \frac{K_I}{\sqrt{2\pi r}} \cos \frac{\theta}{2} \left( 1 - \sin \frac{\theta}{2} \sin \frac{3\theta}{2} \right) )</td>
<td>( \frac{K_{II}}{\sqrt{2\pi r}} \sin \frac{\theta}{2} \left( 2 + \cos \frac{\theta}{2} \cos \frac{3\theta}{2} \right) )</td>
<td>( \frac{K_I}{\sqrt{2\pi r}} \sin \frac{\theta}{2} \cos \frac{\theta}{2} \cos \frac{3\theta}{2} )</td>
</tr>
<tr>
<td>Mode II</td>
<td>( \frac{K_{II}}{\sqrt{2\pi r}} \sin \frac{\theta}{2} \cos \frac{\theta}{2} \cos \frac{3\theta}{2} )</td>
<td>( \frac{K_{II}}{\sqrt{2\pi r}} \sin \frac{\theta}{2} \left( 1 - \sin \frac{\theta}{2} \sin \frac{3\theta}{2} \right) )</td>
<td>( \frac{K_I}{\sqrt{2\pi r}} \left( 1 - \sin \frac{\theta}{2} \sin \frac{3\theta}{2} \right) )</td>
</tr>
</tbody>
</table>

\( \sigma_{zz} = \nu(\sigma_{xx} + \sigma_{yy}) \); \( \tau_{xz} = \tau_{yz} = 0 \)

**Table 2.** Displacement Fields in front of Crack Tip for Modes I and II (Anderson, 2017)

<table>
<thead>
<tr>
<th>Mode</th>
<th>( u_x )</th>
<th>( u_y )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mode I</td>
<td>( \frac{K_I}{2\mu} \sqrt{\frac{r}{2\pi}} \cos \frac{\theta}{2} \left( \kappa - 1 + 2 \sin^2 \frac{\theta}{2} \right) )</td>
<td>( \frac{K_{II}}{2\mu} \sqrt{\frac{r}{2\pi}} \sin \frac{\theta}{2} \left( \kappa + 1 + 2 \cos^2 \frac{\theta}{2} \right) )</td>
</tr>
<tr>
<td>Mode II</td>
<td>( \frac{K_I}{2\mu} \sqrt{\frac{r}{2\pi}} \sin \frac{\theta}{2} \left( \kappa + 1 + 2 \cos^2 \frac{\theta}{2} \right) )</td>
<td>( \frac{K_{II}}{2\mu} \sqrt{\frac{r}{2\pi}} \cos \frac{\theta}{2} \left( \kappa - 1 + 2 \sin^2 \frac{\theta}{2} \right) )</td>
</tr>
</tbody>
</table>

The symbols in the Tables are as follows: \( \nu \) denotes Poisson’s ratio, \( E \) signifies modulus of elasticity, \( \kappa \) denotes Kolosov constant and \( \mu \) denotes the shear modulus. \( \kappa \) and \( \mu \) can be written as:

\[
\kappa = (3 - 4\nu) \quad \text{Plane strain} \\
\kappa = \frac{(3 - \nu)}{(1 + \nu)} \quad \text{Plane stress} \\
\mu = \frac{E}{2(1 + \nu)}
\]

(24) (25) (26)
4. Results and discussion

The first example considered straight edge configuration shown in Figure 1 by comparing XFEM results with the closed form solution as proposed in (Tada et al., 2000).

\[ K_I = f \sigma_0 \sqrt{\pi a} \]
\[ f = 1.122 - 0.231(a/L) + 10.55(a/L)^2 - 21.72(a/L)^3 + 30.382(a/L)^4 \]  

(27)

In this example the mixed mode SIFs \((K_I, K_{II})\) are computed using domain based interaction integral (Moran and Shih, 1987; Sukumar et al., 2000). Firstly, normalized SIF \((K_I)\) with respect to \(a/L\) ratio for horizontal edge crack \((\beta=0 \text{ and } d/D=0)\) was estimated and the result compared with that of the closed form solution from reference (Tada et al., 2000). From Fig. 4, the theoretical results are in agreement with the present result.

![Fig. 4. Comparative study on the variation of Normalized SIF with normalized crack length (Tada et al., 2000)](image)

Fig. 5 and Fig. 6 present the convergence and error estimation for mode-I SIF for different number of nodes respectively. From Fig. 5, the estimated value of \(K_I\) converges to the closed form solution as the number of nodes increases. Similarly the percentage error gets reduced and closer to zero as number of nodes increases, as depicted in Fig. 6. Therefore the number of nodes considered in this study is 50 by 100.

![Fig. 5. Comparative study of \(K_I\) values between XFEM and closed form solution for different number of nodes.](image)
To demonstrate the effectiveness of XFEM, a comparative study between applied stresses ($\sigma_o$) and SIF ($K_I$) has been conducted. SIF is plotted against the applied stress ($\sigma_o$) and it is observed that results from XFEM show good agreement with (Tada et al., 2000) as depicted in Fig. 7. The stress contours $\sigma_{xx}$, $\sigma_{xy}$ and $\sigma_{yy}$ are also shown in Fig. 8 (a), Fig. 8 (b) and Fig. 8 (c) and witnessed that the stress values at the crack tip are maximum as expected.

Fig. 7. Comparative analysis of $K_I$ values with closed form solutions for different values of applied tensile stresses

Fig. 9 and Fig. 10 demonstrate how the normalized crack size ($a/L$) and inclination angle of the crack affect mode I SIFs and mode II SIFs respectively. In this particular example $d/D$ ratio is considered to be 0. As observed from Fig. 9 for each and discrete normalized crack size ($a/L$) mode I SIF decreases and approaches to zero as the crack inclination angle ($\beta$) increases. In other words for each and every inclination angle $\beta$ as crack size increases so does the mode I SIF. It is also noticed from Fig. 9 that the effect of crack inclination angle on the level of increase of the normalized mode I SIF is more dominant at smaller crack angles. For crack inclination angles greater that 60° it is observed that crack size has no significant effect on the normalized SIF ($K_I$), this is possibly due to the decrease in the normal force.
contribution on the crack surface. XFEM result has been compared with results from literature (Fayed, 2017) and good agreements have been observed as in Fig. 9.

![Stress contour for an edge crack](image)

**Fig. 8.** Stress contour for an edge crack

![Normalized mode I SIF vs. crack inclination angle](image)

**Fig. 9.** Effect of crack inclination angle on normalized mode I SIF.

Fig. 10 shows a comparative study among the normalized mode II SIF ($K_{II}$) and crack inclination angle $\beta$. It is clear from Fig. 10 that the values of the normalized mode II SIF ($K_{II}$) escalates from its minimum value zero where $\beta = 0$ to its maximum value and then decline towards zero when $\beta$ approaches $90^\circ$. The normalized mode II SIF ($K_{II}$) attains its maximum value when $\beta$ is between $30^\circ$ and $50^\circ$. Here again, XFEM result has been compared with results from literature (Fayed, 2017) and good agreements has been observed as in Fig. 10. Furthermore Fig. 11 illustrates a comparative study between mode I SIF ($K_{I}$) and crack inclination angle $\beta$. In this example $d/D$ ratio was considered to be 0. It is clearly observed from Fig. 11 that the values of the normalized mode I SIF ($K_{I}$) keeps declining from its maximum value where $\beta = 0$ to its minimum value close to zero when $\beta$ approaches $80^\circ$. Here also a close agreement between XFEM result and results from literature was noticed (Fayed, 2017). Similarly Figs. 12 (a), (b) and (c) show stress contours $\sigma_{xx}$, $\sigma_{xy}$ and $\sigma_{yy}$ in the case of inclined crack respectively.
Fig. 10. The effect of crack inclination angle on normalized SIF ($K_{II}$).

Fig. 11. Effect of crack length to width ratio ($a/L$) on normalized SIF ($K_I$).

Fig. 12. Stress contour for an edge crack.
Fig. 13. The effect of crack position on $K_1$ and $K_{II}$, (a) $\beta = 0$, (b) $\beta = 15$ and (c) $\beta = 30$. 
The other parameter we considered in this study was the effect of crack position on the SIFs (I and II) as presented in Fig. 13 for different crack inclination angles and crack size. The results obtained from XFEM have been compared with results from the reference (Fayed, 2017). As it is illustrated in Fig. 13 (a) the change in crack positioning in the vertical axis results in an increase in $K_I$. It is also observed that the rate of increase of $K_I$ is not noticeable for some $d/D$ ratio until a certain $d/D$ ratio for each crack size and inclination angle beyond which it increases faster. This rate of increase in SIF is a function of crack inclination angle and size as it is clearly observed from Fig. 13. The increase in $K_I$ and $K_{II}$ between 0 and 0.6 $d/D$ ratio when $a/L=0.1$ is not noticeable whereas at $a/L$ ratio of 0.8 and above it attains its maximum value. But in case of $a/L$ ratio of 0.3 and 0.5 the increase in SIF ($K_I$ and $K_{II}$) become more noticeable at higher angles.

5. Conclusions

Extended Finite Element Method (X-FEM) was implemented in this study for estimation of crack propagation in a material. The approach employed in this study is extremely vital due to the fact that it does not require multiple remeshing which is quite mandatory in the case of FEM when the cracks start moving. In this article, tensile load has been applied on the top face of a slanted edge cracked plate remotely to compute the mixed mode SIFs ($K_I/K_{II}$). The effects of different parameters like cracking angle and its location, crack position along the vertical axis and crack length to width ratio ($a/L$) have been considered in the determination of SIFs. By taking into account the aforementioned parameters, the mixed mode SIFs ($K_I/K_{II}$) has been determined. The results obtained from XFEM remarkably agreed with those from literature and hence justified the prominent performance of the method to compute SIF for mode I and mode II.

References


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